



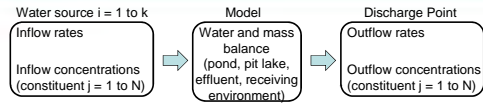
IMWA 2010, Sydney, Nova Scotia, Canada, September 5 to 9

### Mine Water Characterization for Probabilistic Modelling and Uncertainty Analysis

By Nicolas Lauzon

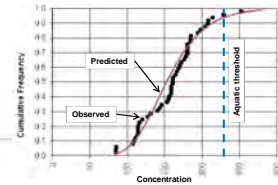


### Water Quality Modelling

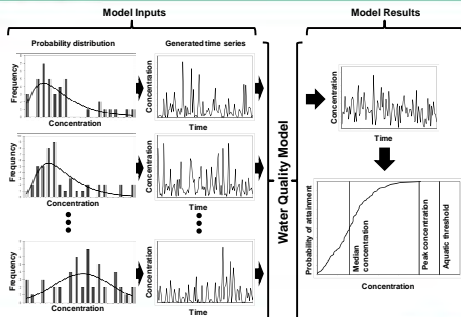


**Issue:** Limited number of water samples to characterize source loadings

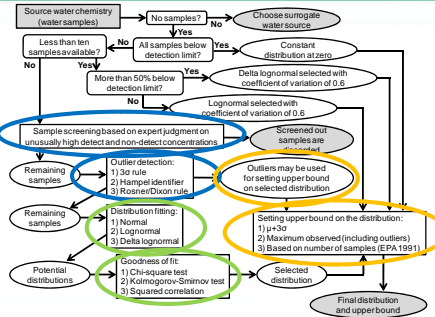
**Objective:** Defining the realistic range of outflow concentrations



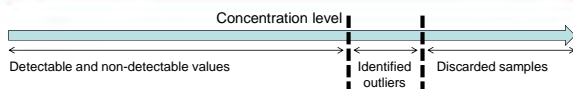
### Probabilistic Water Quality Modelling Structure



### Processing of Water Sample Concentration Data



### Data Description

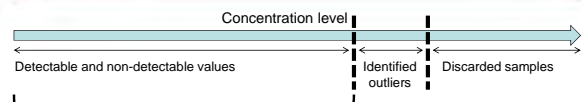


**Discarded samples:** Selected based on expert judgment (unusually high detectable and non-detectable values)

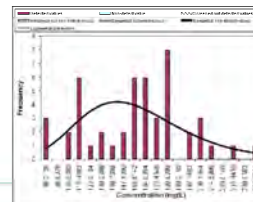
**Identified outliers:** Identification from a pool of acknowledged detection methods (e.g. 3σ rule, Hampel identifier, Rosner/Dixon rule). A value is considered an outlier only if all methods provide a positive diagnostic, or from expert judgment.

**Iterative process:** Loop, starting with no discarded sample, with step by step refinement (judgment calls on outliers and discarded samples).

### Distribution Fitting



Data used for fitting a probability distribution



**Typical distributions (EPA 1991):**

- Normal
- Lognormal
- Delta lognormal

**Goodness of fit (pool of methods):**

- Chi-square test
- Kolmogorov-Smirnov test
- Square correlation
- Visual inspection

### Selection of a Maximum Bound

Concentration level

← Detectable and non-detectable values      Identified outliers      Discarded samples →

Data used for determining the maximum bound applied to the fitted distribution.

Determined from a pool of methods:

- $\mu+3\sigma$
- Maximum observed, including outliers
- Based on the number of sample (EPA 1991)

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### Mine Water Processor

Main menu

Distribution fitting

Data description

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### Water Quality Uncertainty Analysis Model

PROCESSES      FLOW      INPUT WATER QUALITY

Water Quality Model

90% percentile lower confidence limit  
Designed scenario  
90% percentile upper confidence limit

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### Defining Uncertainty on Concentrations

**Standard deviation:**

Realizations of  $s_{obs} : s_{obs,1} + s_{obs,2} + \dots + s_{obs,N}$

$$s_{obs,i} = (Fs_{obs}^2)^{0.5}$$

Where  $F$  is the Fisher distribution

**Mean:**

Realizations of  $\bar{x}_{obs} : \bar{x}_{obs,1} + \bar{x}_{obs,2} + \dots + \bar{x}_{obs,N}$

$$\bar{x}_{obs,i} = \bar{x}_{obs} + T \left( \frac{s_{obs}^2 + s_{obs,i}^2}{n_{obs}} \right)^{0.5}$$

Where  $T$  is the Student's distribution

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### Conclusion

- Gaining confidence in the prediction of concentrations of mine outflows or receiving environment
- Defining source loadings within realistic ranges from observed samples
- Expert judgment for the generation of concentrations that are conservative but not unrealistic given the existing knowledge of the source waters
- Characterization of uncertainties

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### Acknowledgment

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**Questions?**

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